

## Virtual 3D microstructures with specified characteristics of state variable distributions

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Introduction  
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Framework  
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Grains  
○○○○○

Texture  
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Results  
○○○

Final words  
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# Outline

Introduction

Framework

Grains

Texture

Results

Final words

## Physical model

is “a representation of the essential aspects of an existing system (or a system to be constructed) which presents knowledge of that system in usable form”<sup>a</sup>

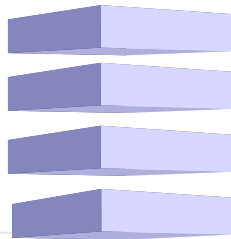
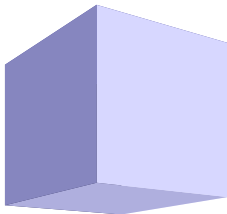
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<sup>a</sup>*Eykhoff*, System Identification: Parameter and State Estimation (1974).

# Motivation

## 3D measurements

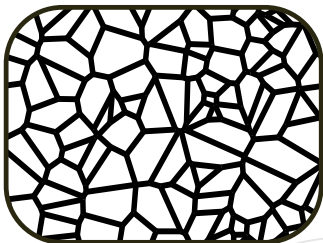
of real materials are possible but consume relatively high amount of financial and time resources. Which implies in volume/statistics limitation.



# Virtual Materials

## Virtual material

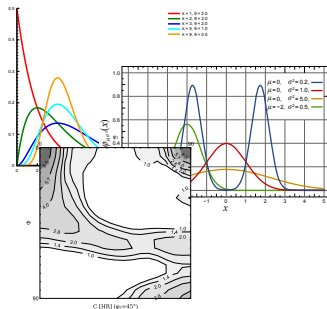
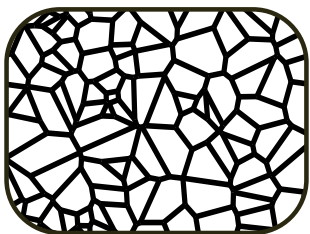
is an abstraction that represents characteristics of a microstructure in a computer data structure.



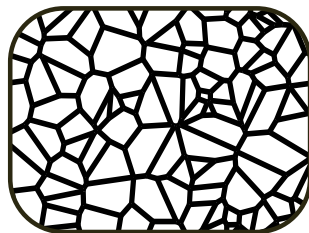
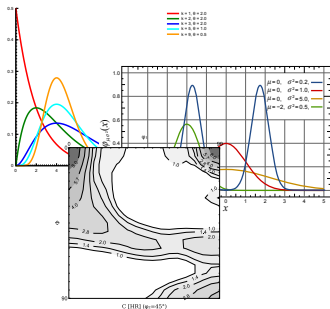
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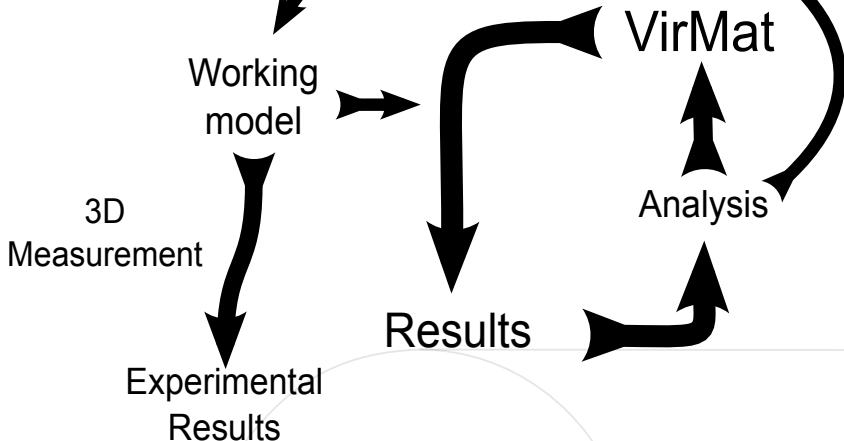
## In the past decades ...



... but now we want the reverse!



# Our Solution





## Grain Morphology

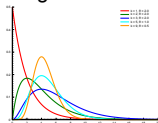
shape distribution

number of neighbours

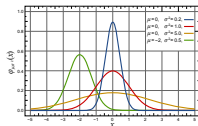
size distribution

clustering

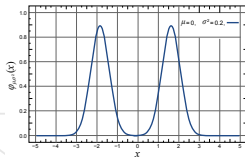
log-normal



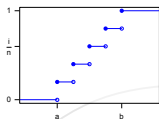
normal



bimodal



discrete or custom



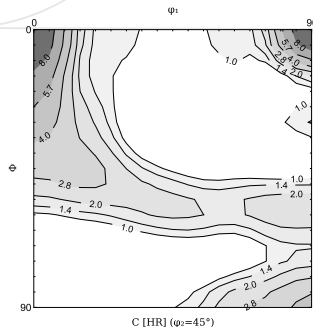
# Texture

## Orietation distribution

$$\frac{dV}{V} = f(g)dg$$

$$\oint f(g)dg = 1$$

$$f(g) = \sum_{l=0}^{\infty} \sum_{m=-l}^l \sum_{n=-l}^l C_l^{mn} \cdot T_l^{mn}(g)$$



At first glance, both *Grain Morphology and Texture*, are independent ....  
... but:

- 1 volume fraction constraint is implicit
  - no random texture with 2 grains
- 2 and...

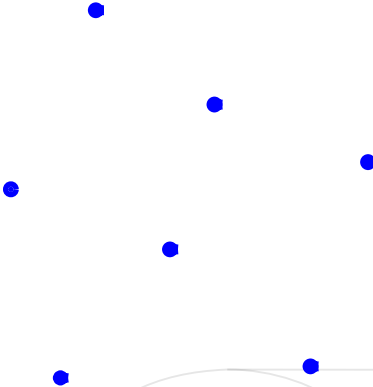
**Grain  
Morphology**



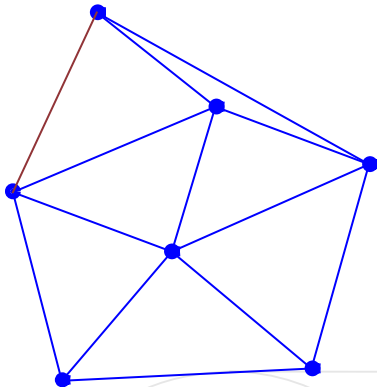
**Texture**

**Grain Boundary  
Character Distribution**

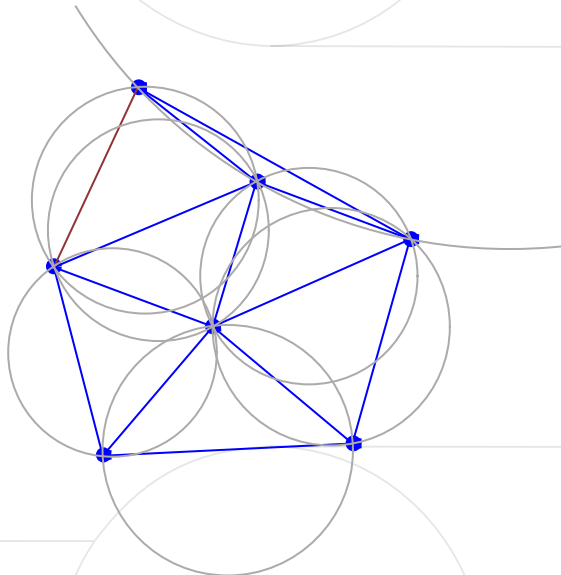
# Space Partition



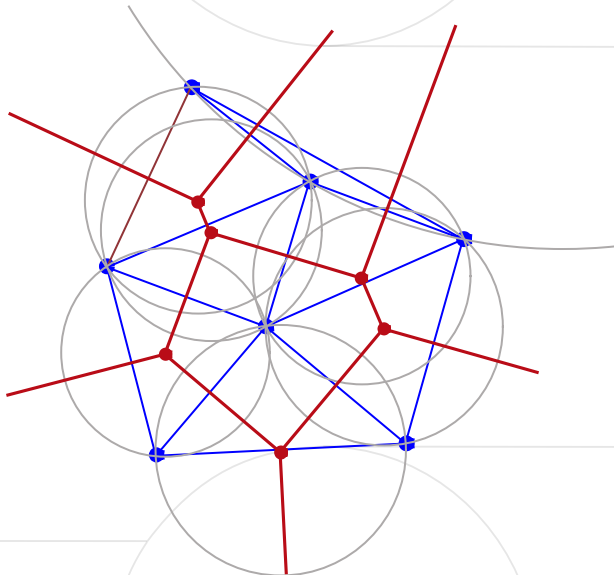
# Space Partition



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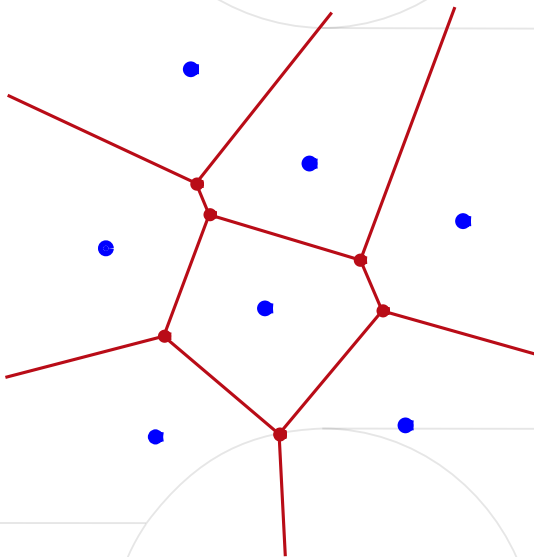


# Space Partition

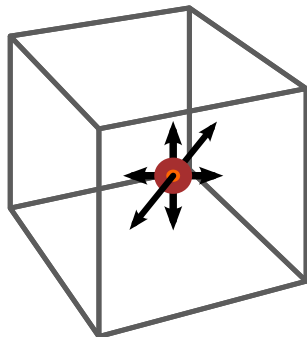
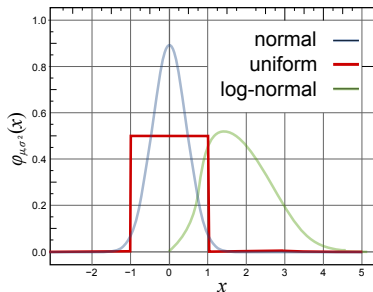


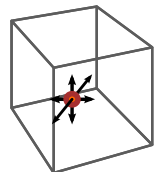
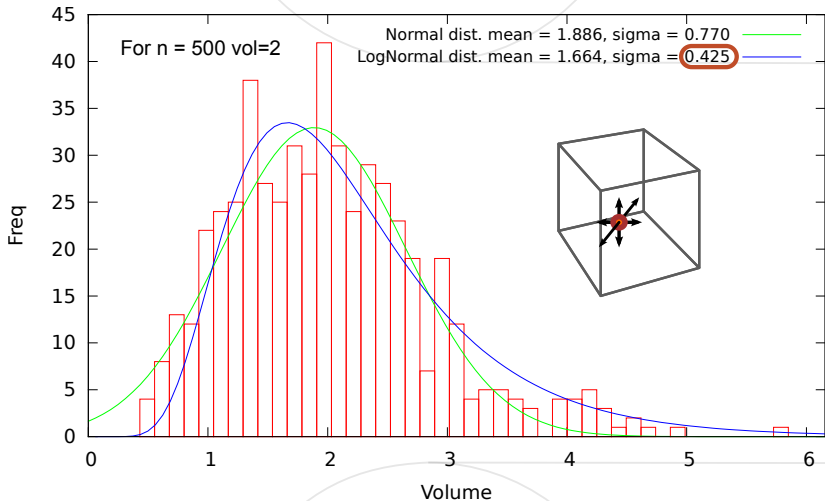


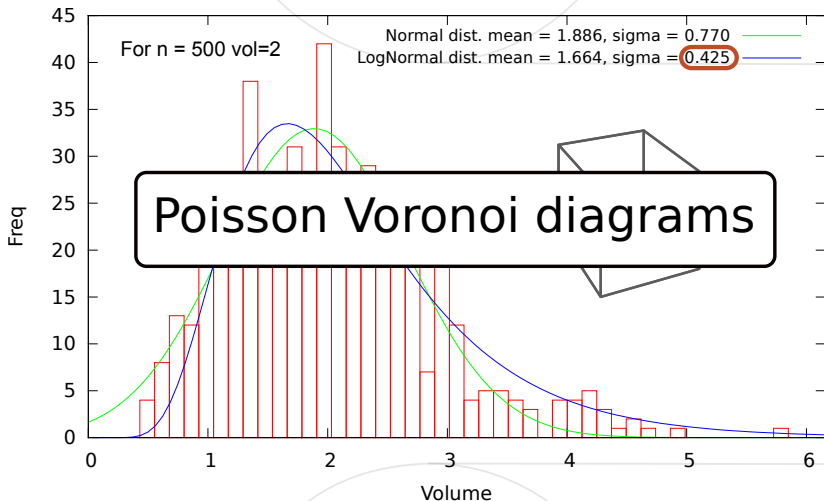
# Space Partition

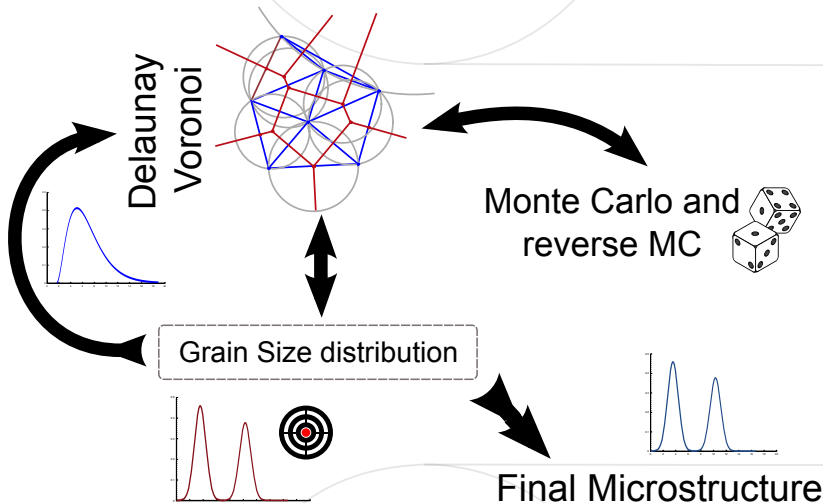


# Uniform Random distribution

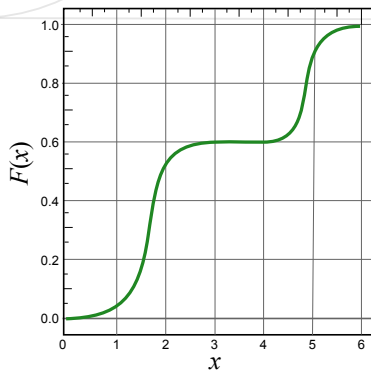
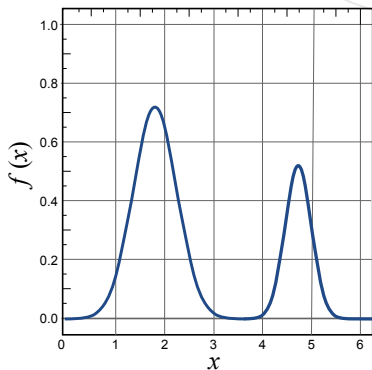






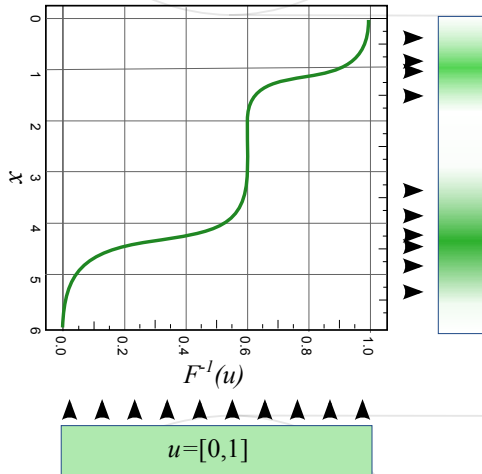


# Orientation sampling



$$F(x) = \int_{-\infty}^x f(t) dt$$

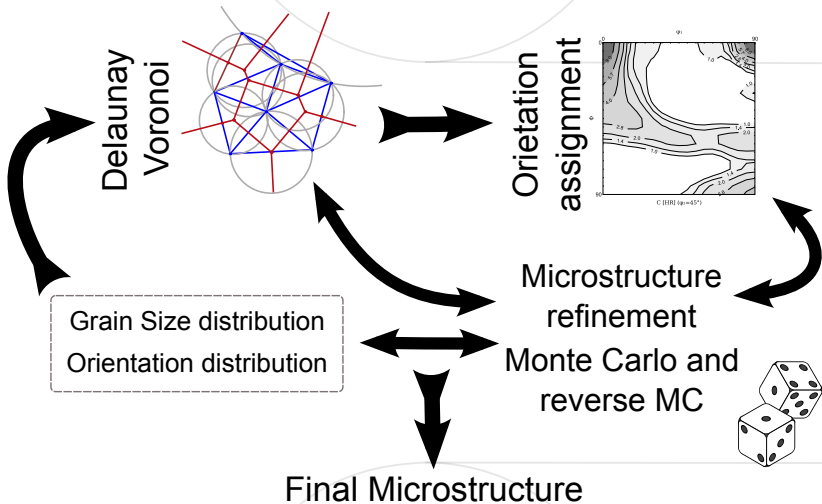
# Orientation sampling



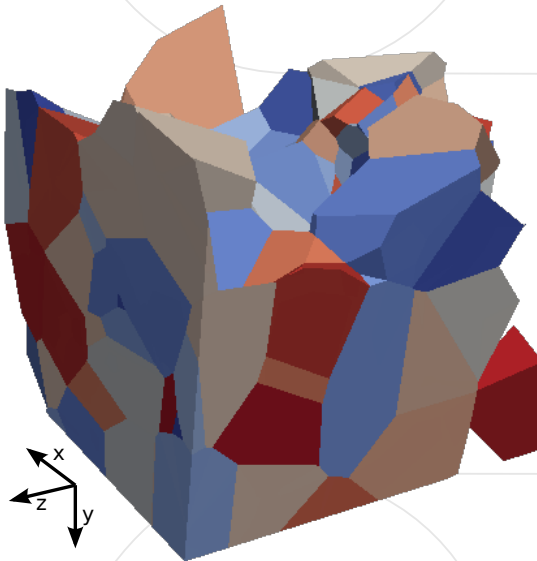
## Attention

sampling an ODF return values unrelated with the grain size distribution.  
All sampled values are valid for constant grain size.



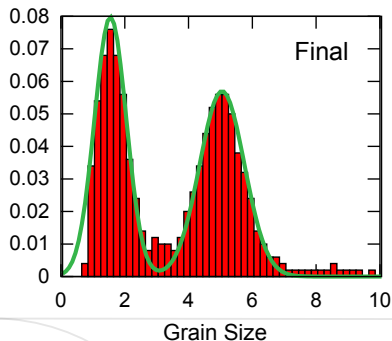
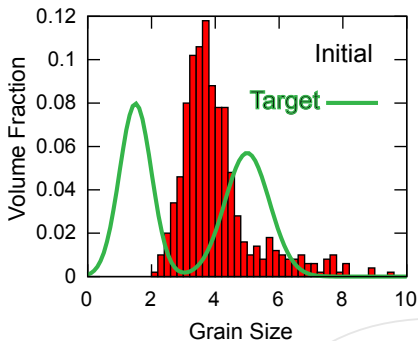


# Grain Morphology



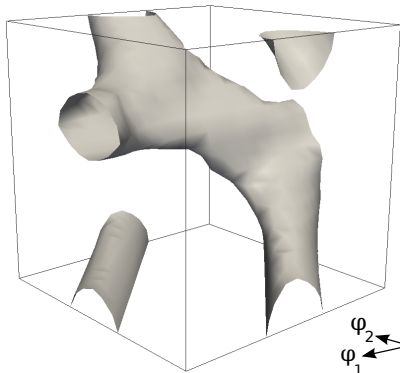
# Grain Size Distribution

## Histogram

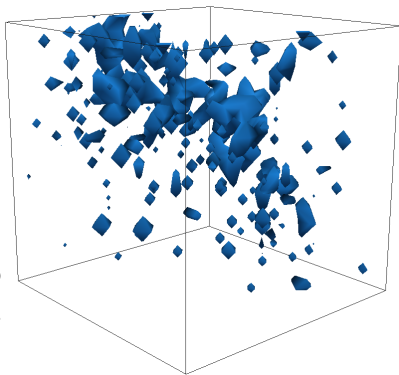


# Orientation Distribution

Target 

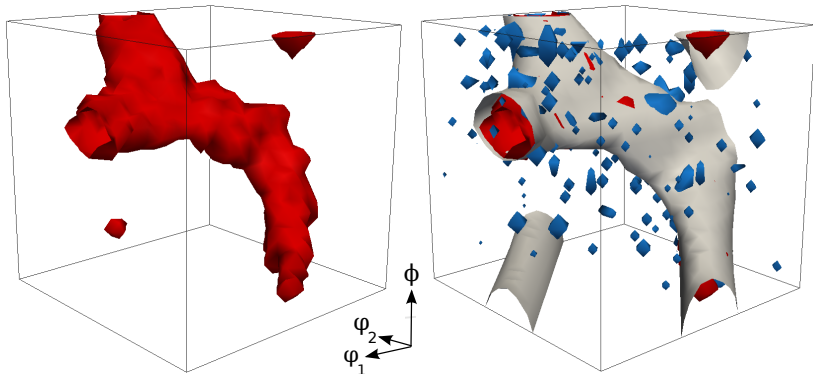


Initial sampling



# Orientation Distribution

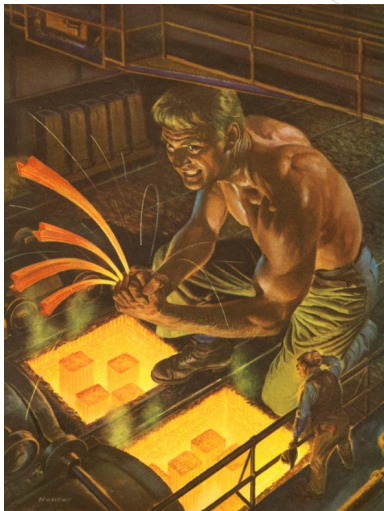
## Final



## Future work

- 1 Faster algorithm for grain generation with control of others properties other than size distribution.
- 2 Sampling orientations regarding grain size distribution.
- 3 Merge distributions into a high dimension distribution function (DF).
- 4 Sampling set of properties from high dimensions DF.

# Thank for your attention !!!



*“Joe Magarac was an imaginary folk hero whose story came from eastern European immigrants working in Pittsburgh area steel mills. His physical power and his brave, generous, and hard-working character made Joe Magarac (whose name “Magarac” means “donkey” in Croatian) the greatest steelworker who ever lived.”<sup>a</sup>*

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<sup>a</sup>[http://www.jaha.org/edu/discovery\\_center/work/folk\\_hero.html](http://www.jaha.org/edu/discovery_center/work/folk_hero.html)